3 (Sem-6/CBCS) PHY HE 3

2023 PHYSICS

(Honours Elective)

Paper: PHY-HE-6036

(Advanced Mathematical Physics-II)

Full Marks: 80

Time: Three hours

The figures in the margin indicate full marks for the questions.

1. Answer any ten of the following:

1×10=10

- (a) State Hamilton's Principle.
- (b) Define Generalized co-ordinates.
- (c) What is meant by a Geodesic?

- (d) Generalized coordinates are:
 - (i) Independent
 - (ii) Dependent
 - (iii) Spherical polar coordinates
 - (iv) None of the above
- (e) A particle is moving doing the arc of a circle. The suitable generalized coordinate (s) is/are:
 - (i) ronly
 - (ii) θ only
 - (iii) r and θ both
 - (iv) x and y
- (f) For a conservative system, the potential energy does not depend upon:
 - (i) force
 - (ii) generalized velocity
 - (iii) generalized coordinator
 - (iv) All of the above

- (g) For a conservative system Hamiltonian represents:
 - (i) T+V
 - (ii) T-V III adorg 1 Janw (ii)
 - (iii) L + V
 - (iv) 2T-V
- (h) If the Lagrangian of a system does not depend on time explicitly, then:
 - (i) the Hamiltonian can not be constant
 - (ii) the Hamiltonian is constant
 - (iii) potential energy is constant
 - (iv) kinetic energy is constant
- (i) The shortest distance between two points in a plane is:
 - (i) an arc of a circle
 - (ii) an arc of ellipse
 - (iii) a straight line leaded at
 - (iv) arbitrary arc

- (j) What is Mutually Exclusive Events?
 - (k) Give an example of Collectively Exhaustive events.
 - (1) What is Probability Distribution Function?
 - (m) What is Compound Probability?
- (n) Define Cyclic group.
- 2. Answer any five of the following: 2×5=10
 - (a) Write Euler Lagrange's differential equations.
 - (b) Explain Principle of List action.
 - (c) What do you mean by canonical coordinates?
 - (d) What do you mean by Lagrangian and Hamiltonian?
 - (e) Define Mathematical Probability and Statistical Probability.
 - (f) Define relation and mapping,

- (g) What are Homomorphism and Isomorphism of group?
- (h) If $A = \{4, 5\}$ and $B = \{1, 2, 3\}$ are two sets, then find their Cartesian products $A \times B$ and $B \times A$.
- 3. Answer any four of the following: 5×4=20
 - (a) Find the equation of a motion of a simple pendulum using Lagrange's equation.
 - (b) What are Poisson Brackets and Lagrange Brackets? Prove that both of them do not obey the commutative law of algebra.
 - (c) Define a group and state its postulates.
 - (d) Show that in a group G, identity elements e is unique.
 - (e) Show that a non empty subset H of a group G is a subgroup of G iff
 - (i) $a, b \in H \Rightarrow ab \in H$
 - (ii) $a \not\models H \Rightarrow \alpha^1 \in H$

- probabilities of two Mutually Exclusive
 Events A and B then the probability of
 either of them is P (A or B) = P (A) + P (B).
- 4. Answer any four of the following: 10×4=40

Curtesian products AxB

- that the shortest distance between two fixed points in a plane is a straight line.
- (b) Use Hamilton's Principle to find the equation of motion of one dimensional harmonic oscillator. What is modified Hamilton's Principle? 7+3=10
- (c) Show that a non empty subset H of a group G is a subgroup of G iff
 - (i) $a, b \in H \Rightarrow ab \in H$
 - (ii) $a \in H \Rightarrow \alpha^{-1} \in H$ 5+5=10
 - (d) Show that under canonical transformation, Poisson-Bracket is invariant.
 - (e) What is the law of Conditional Probabilities? State and prove Bayes' theorem. 4+6=10

(f) What is Random Variable? Explain about probability distribution of a discrete random variable and a continuous random variable.

2+4+4=10

- (g) What is Normal Distribution? Explain with schematic diagrams that how the shape of Normal Distribution curves depends upon the Mean and Standard Deviation. Write importance of Normal Distribution. 2+6+2=10
- (h) Explain the Poisson distribution. Consider an emergency room of a hospital where the past records indicate an average of 5 arrivals daily. The demand for emergency room service at this hospital is distributed according to a Poisson distribution. Calculate the probability of exactly 0, 1, 2, 3, 4 and 5 arrivals. What is the probability of more than 3 arrivals?